

**\*VHF - VERY HIGH FREQUENCY**

**\*RREA - RELATIVISTIC RUNAWAY ELECTRON AVALANCHE**

# **SIMULATION OF VHF SIGNAL FROM RREA**

**Khamitov Timur , MIPT**

# GOAL

## Aragats antennas

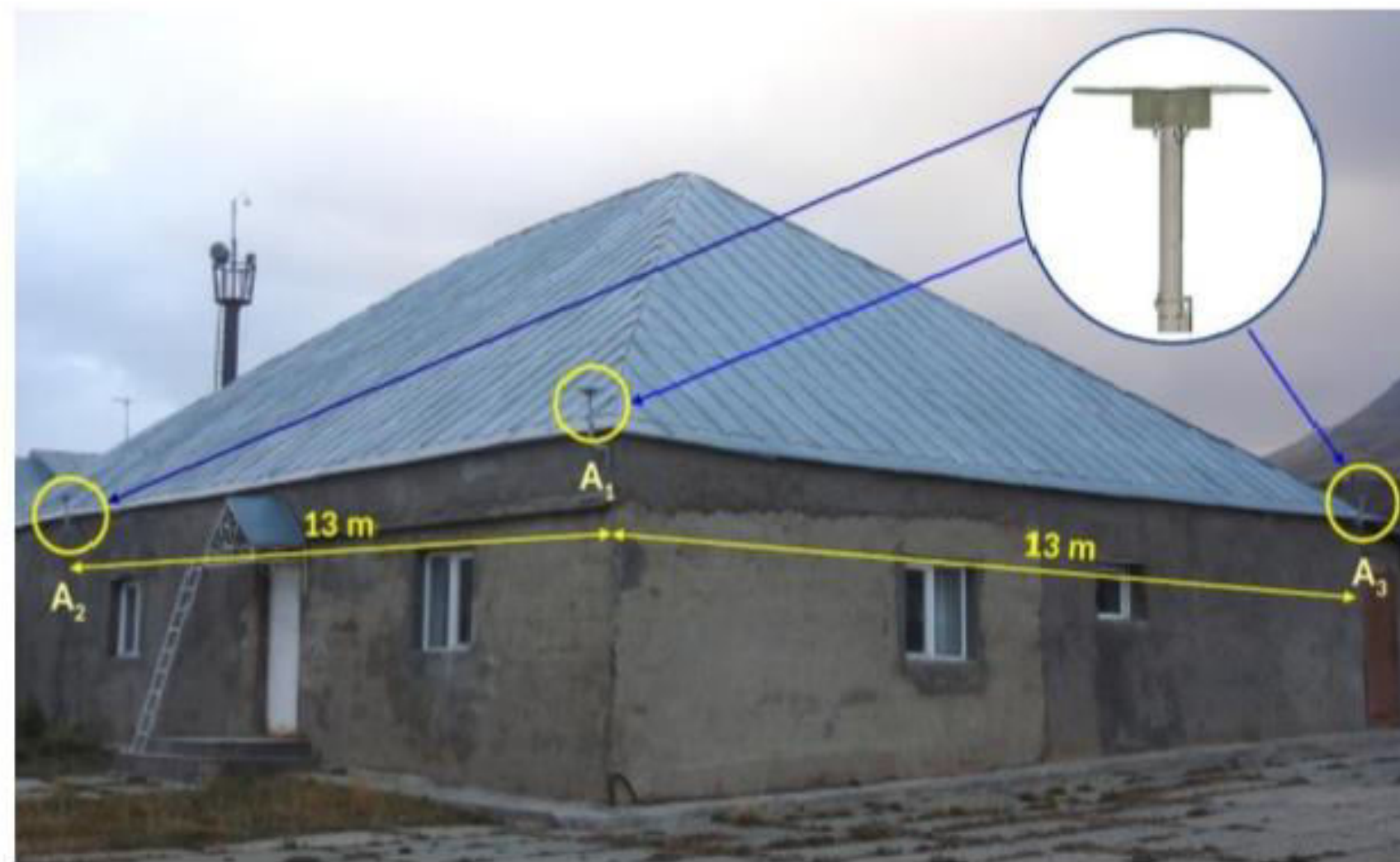
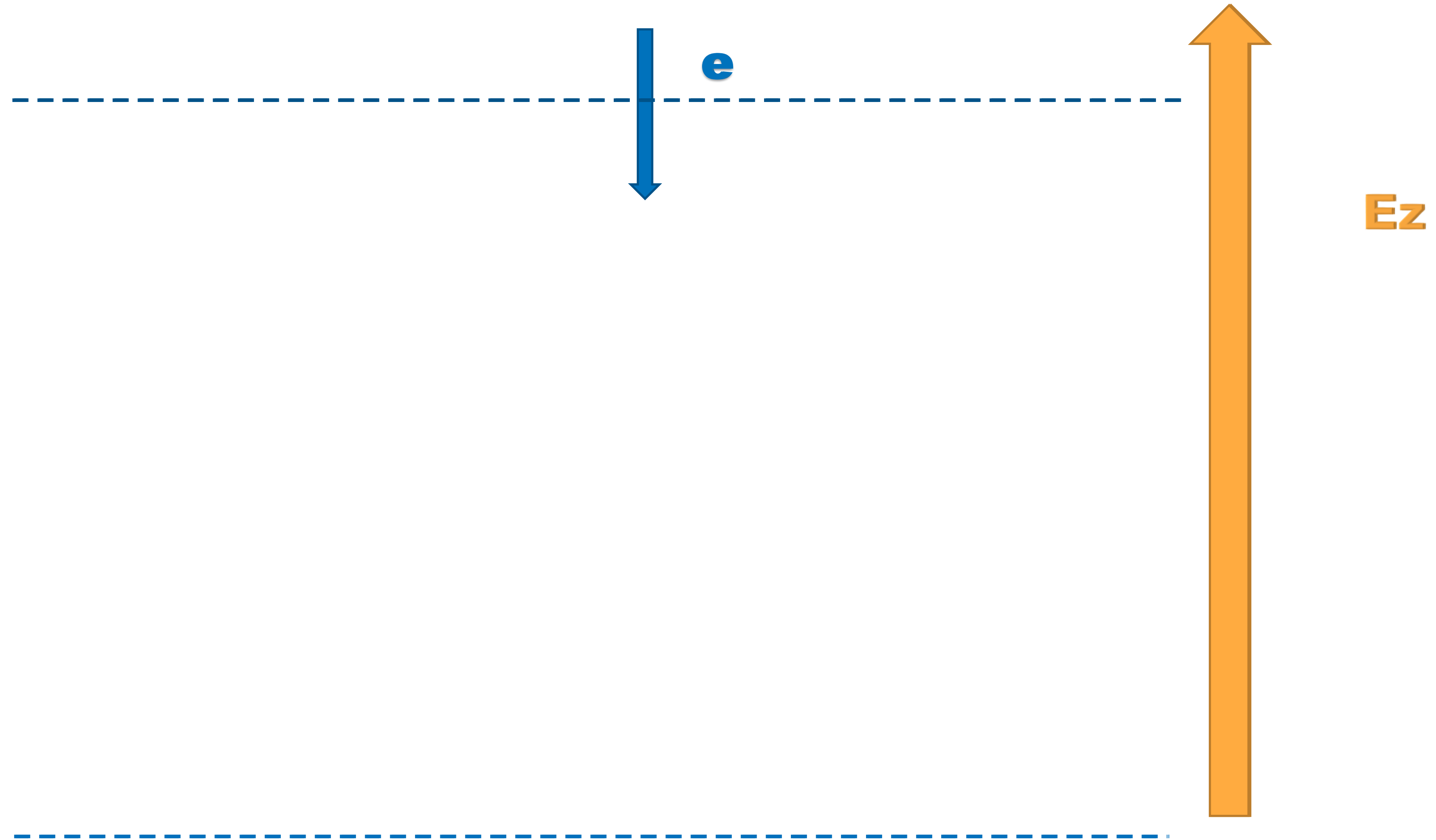


Image credits to CRD, YerPhI.

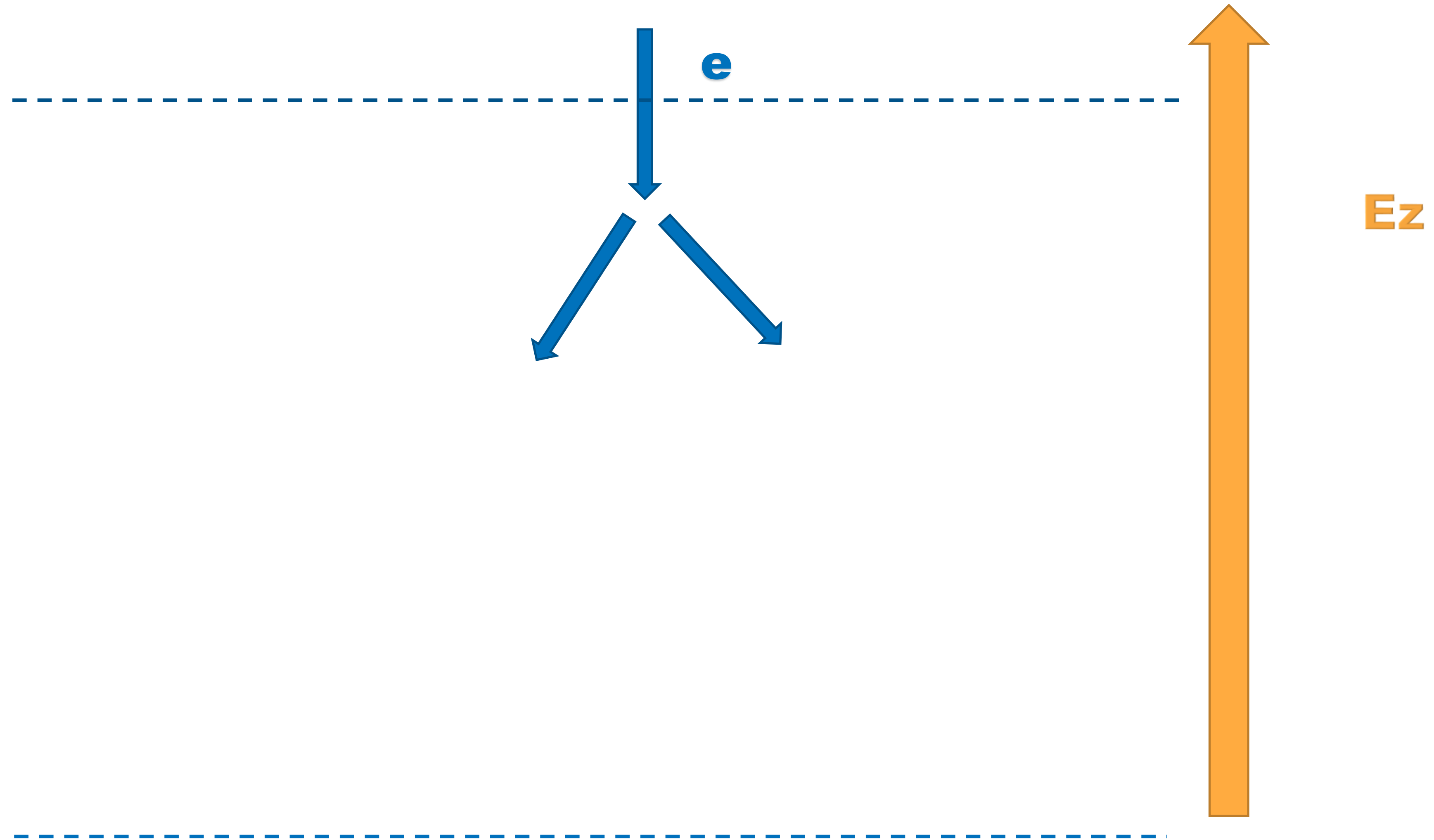


A. Kiselyov, M. Dolgonosov, S. Soghomonyan, V. Karedin

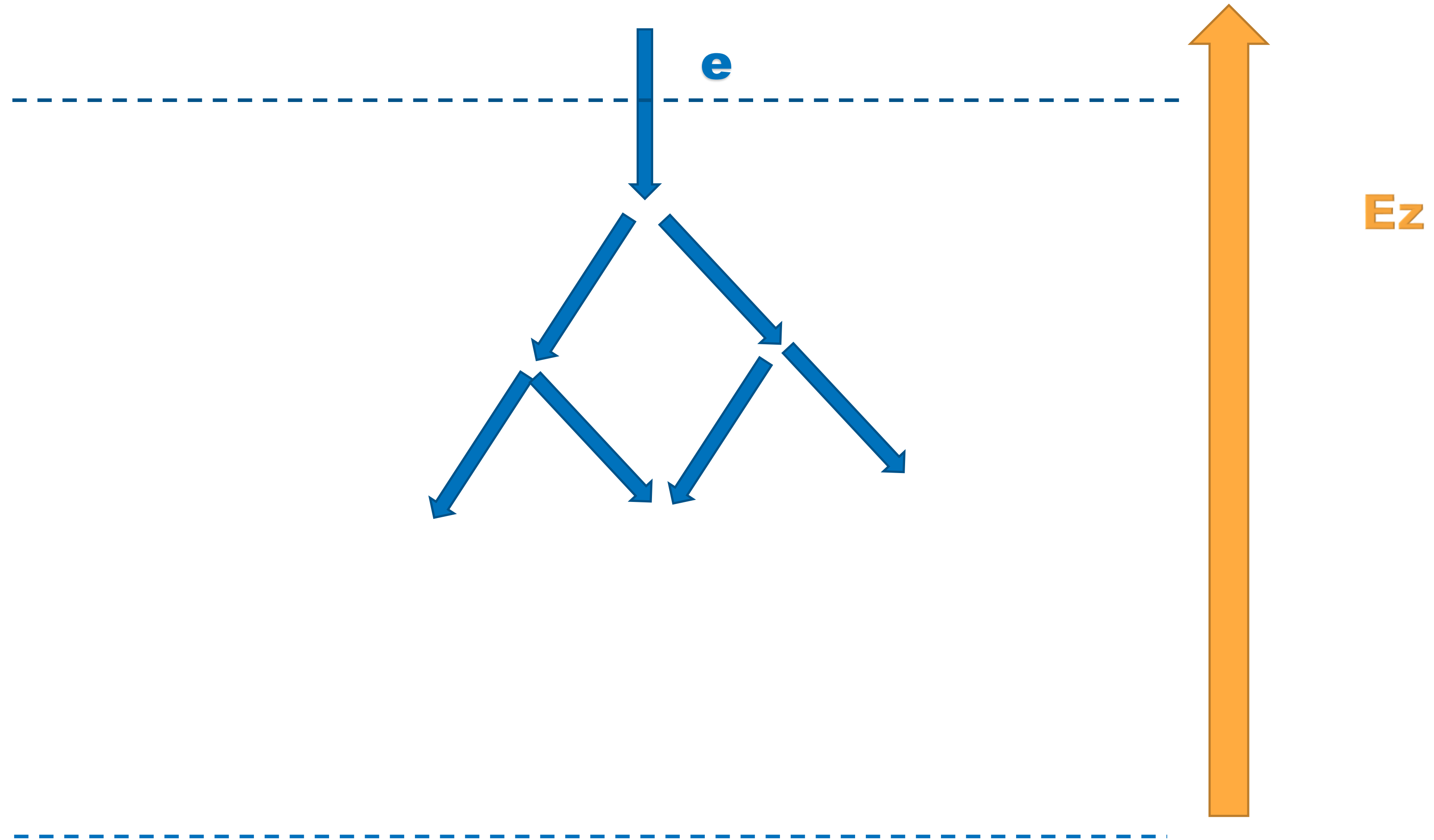
# RELATIVISTIC RUNAWAY ELECTRON AVALANCHE



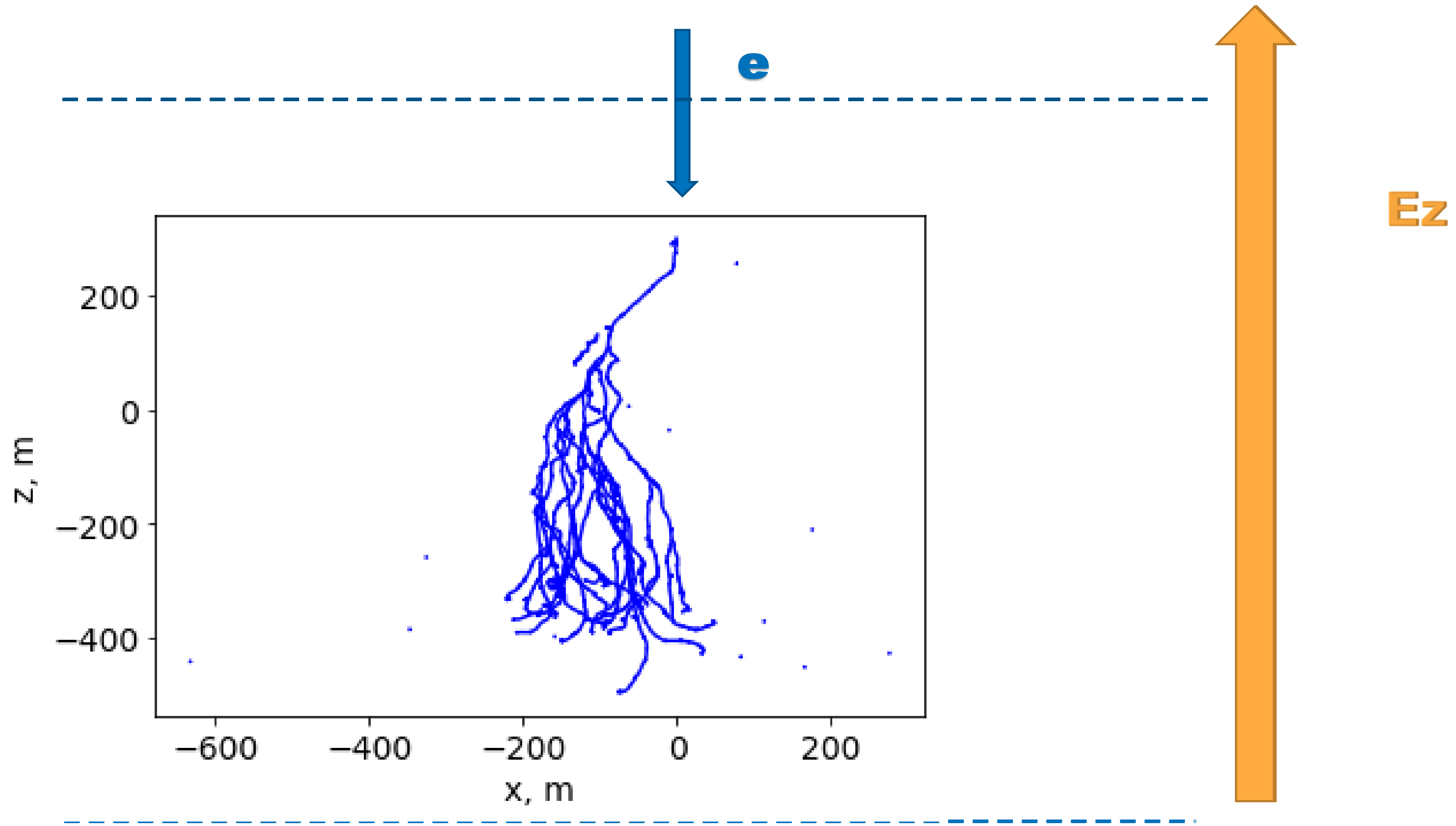
# RELATIVISTIC RUNAWAY ELECTRON AVALANCHE



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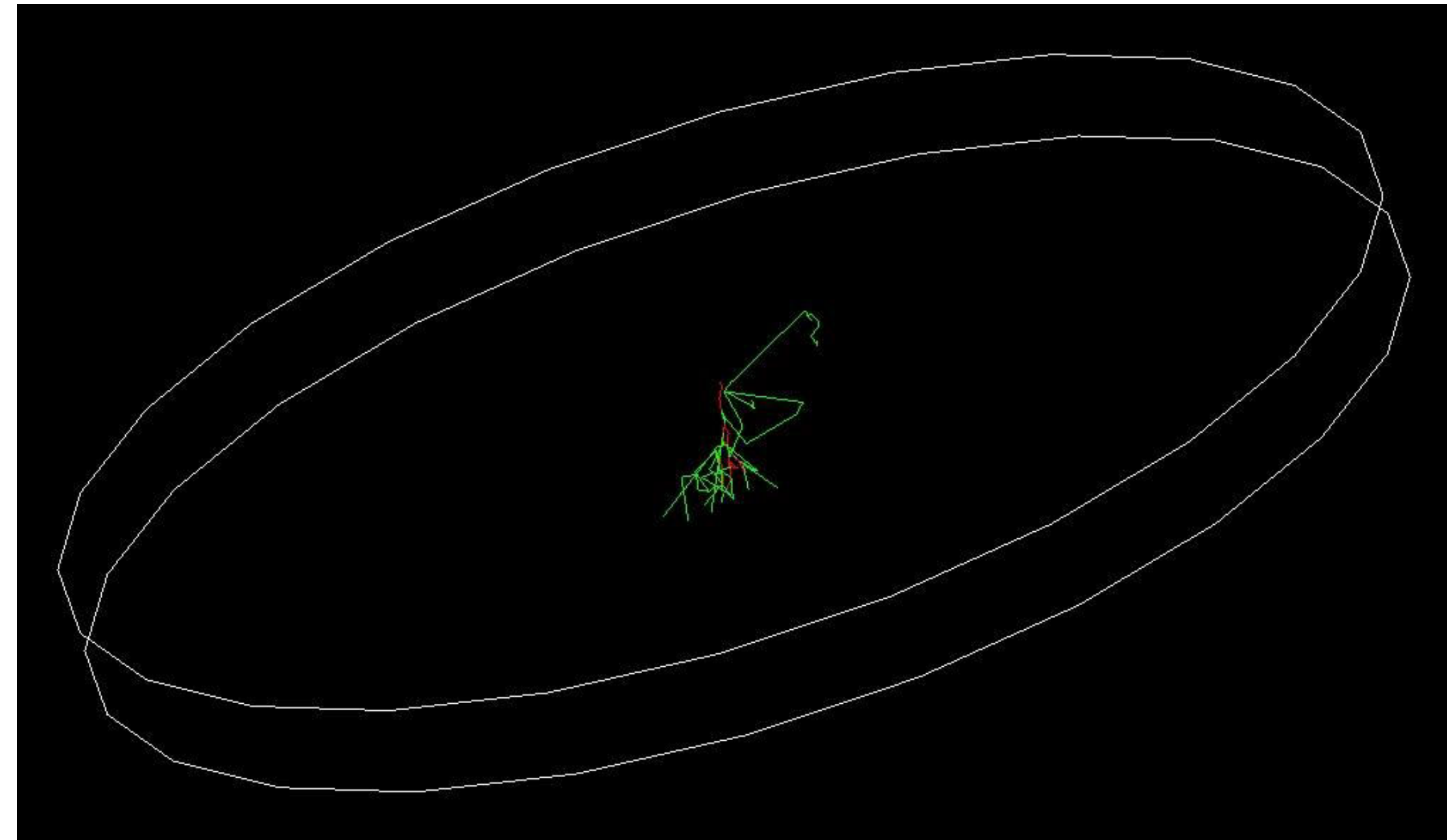
# RELATIVISTIC RUNAWAY ELECTRON AVALANCHE



# SIMULATION STEP BY STEP



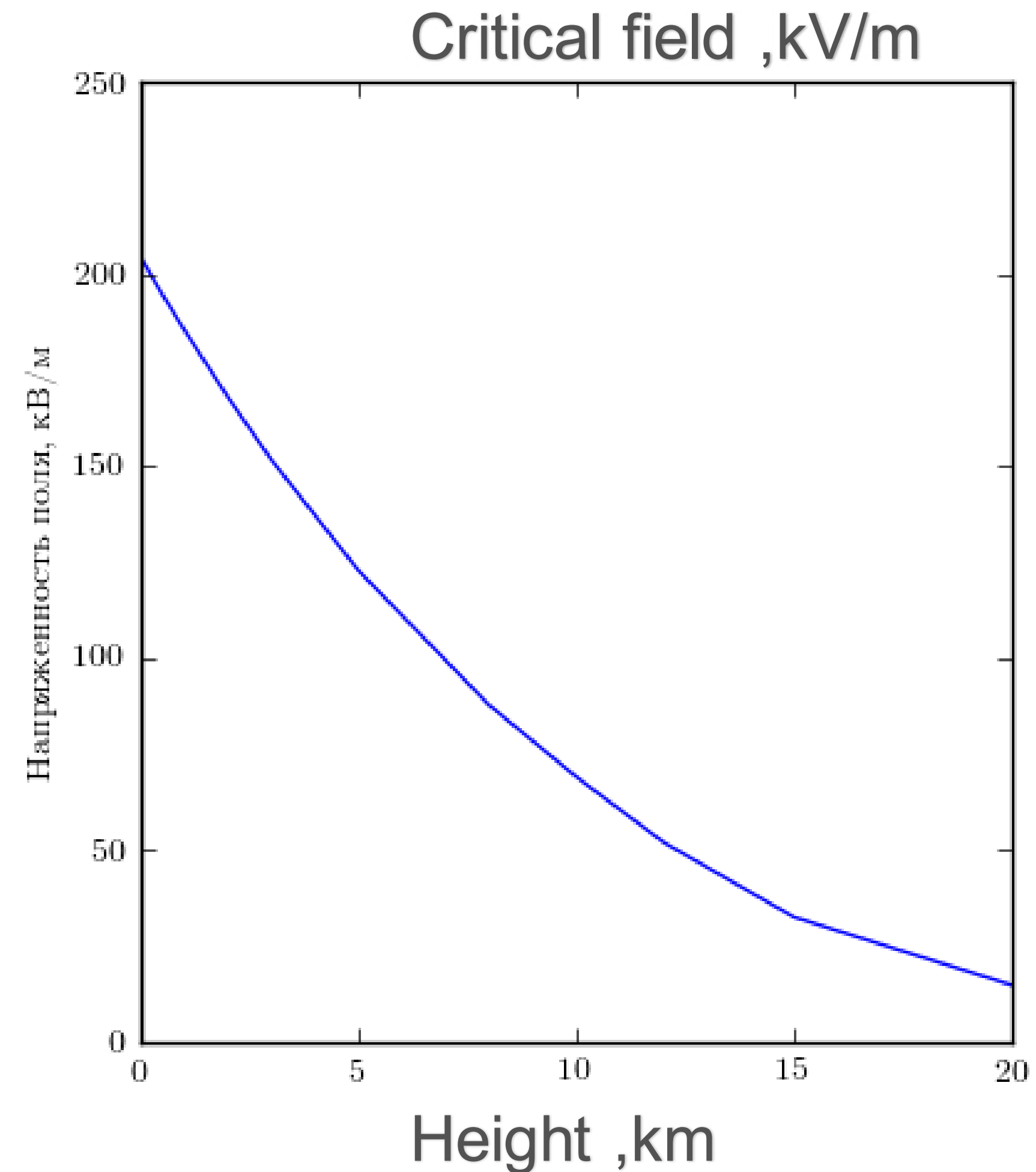
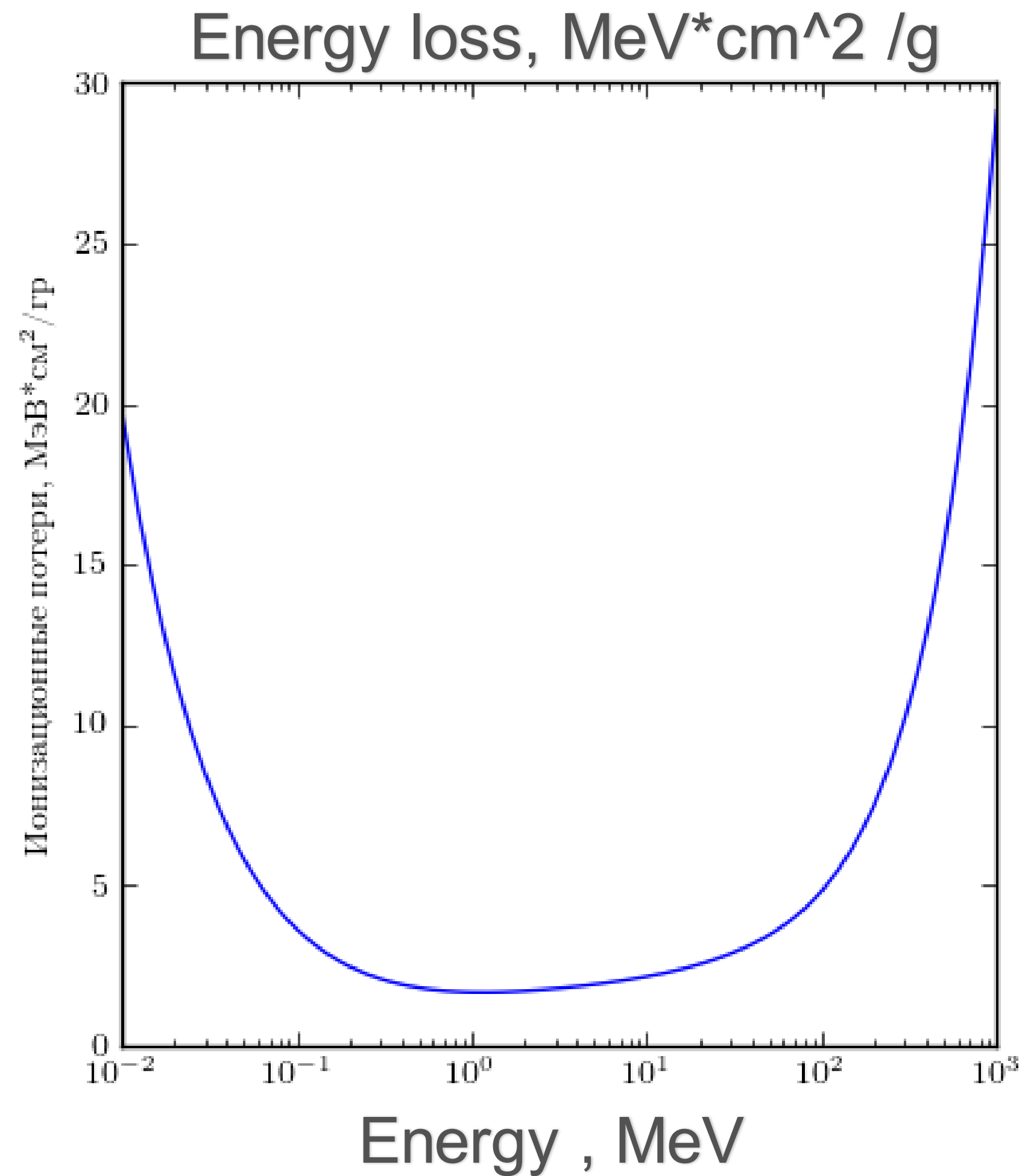
- **Cylinder cell 600m height**
- **Placed at 10 km height**
- **30 keV energy cut**
- **Cylinder is very wide (10 km)**
- **Seed electron 3 MeV**
- **Electric field 110 kV/m**



- **A small green line is RREA  
600 m height**

# SIMULATION STEP BY STEP

Gurevich (1992)





# SIMULATION STEP BY STEP



- **Cylinder cell 600m height**
- **Placed at 10 km height**
- **Electric field 110 kV/m**
- **0.03 MeV energy cut**
- **Cylinder is very wide (10 km)**



**COORDINATES  
TIME**



**VELOCITY  
ACCELERATION**



# SIMULATION STEP BY STEP

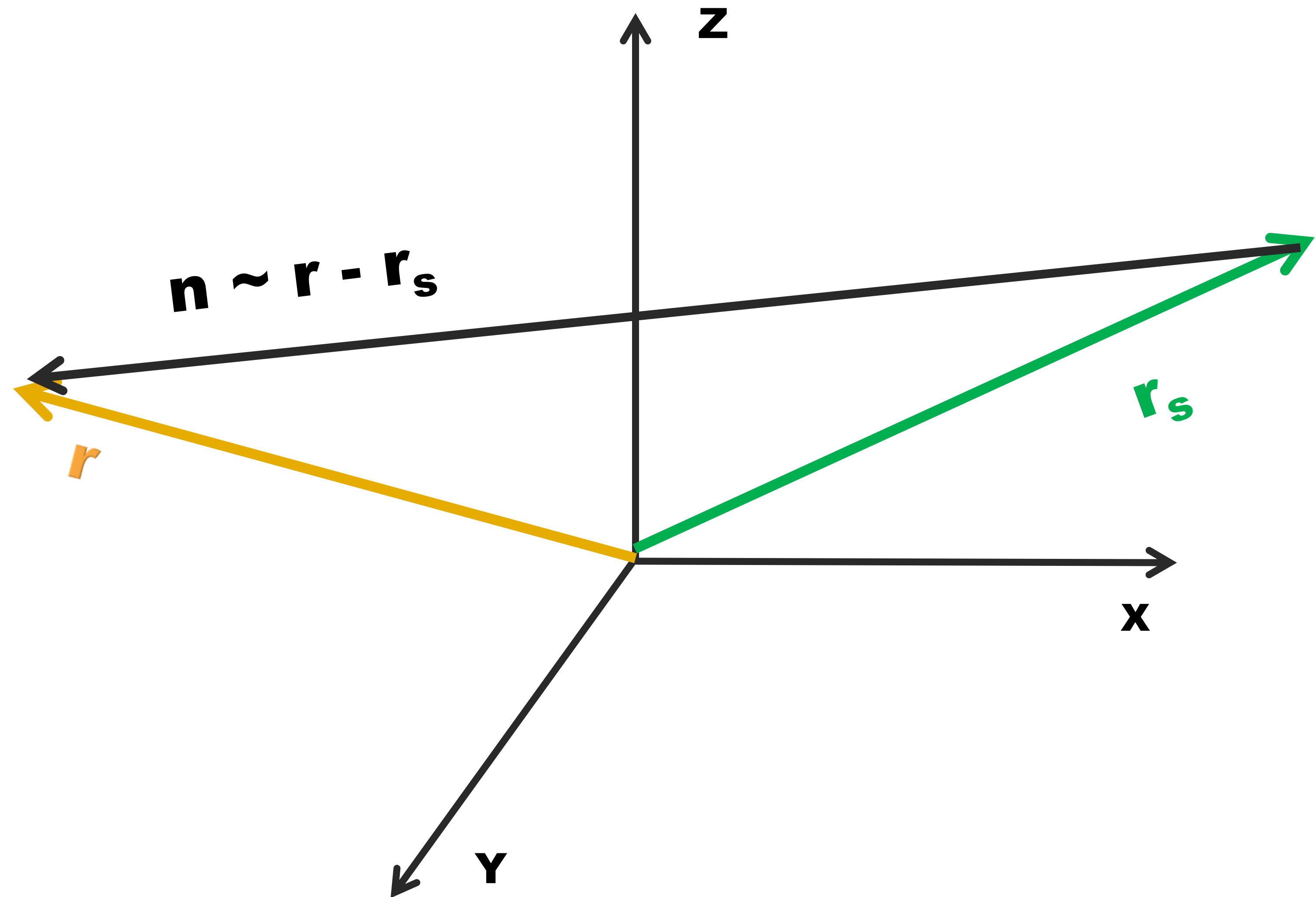
$$\mathbf{E}(\mathbf{r}, t) = \frac{1}{4\pi\epsilon_0} \left( \frac{q(\mathbf{n} - \boldsymbol{\beta})}{\gamma^2(1 - \mathbf{n} \cdot \boldsymbol{\beta})^3 |\mathbf{r} - \mathbf{r}_s|^2} + \frac{q\mathbf{n} \times ((\mathbf{n} - \boldsymbol{\beta}) \times \dot{\boldsymbol{\beta}})}{c(1 - \mathbf{n} \cdot \boldsymbol{\beta})^3 |\mathbf{r} - \mathbf{r}_s|} \right)_{t_r}$$

$$\mathbf{B}(\mathbf{r}, t) = \frac{\mu_0}{4\pi} \left( \frac{qc(\boldsymbol{\beta} \times \mathbf{n})}{\gamma^2(1 - \mathbf{n} \cdot \boldsymbol{\beta})^3 |\mathbf{r} - \mathbf{r}_s|^2} + \frac{q\mathbf{n} \times (\mathbf{n} \times ((\mathbf{n} - \boldsymbol{\beta}) \times \dot{\boldsymbol{\beta}}))}{(1 - \mathbf{n} \cdot \boldsymbol{\beta})^3 |\mathbf{r} - \mathbf{r}_s|} \right)_{t_r} = \frac{\mathbf{n}(t_r)}{c} \times \mathbf{E}(\mathbf{r}, t)$$

$$\gamma(t) = \frac{1}{\sqrt{1 - |\boldsymbol{\beta}(t)|^2}} \quad \boldsymbol{\beta}(t) = \frac{\mathbf{v}_s(t)}{c}$$

# SIMULATION STEP BY STEP

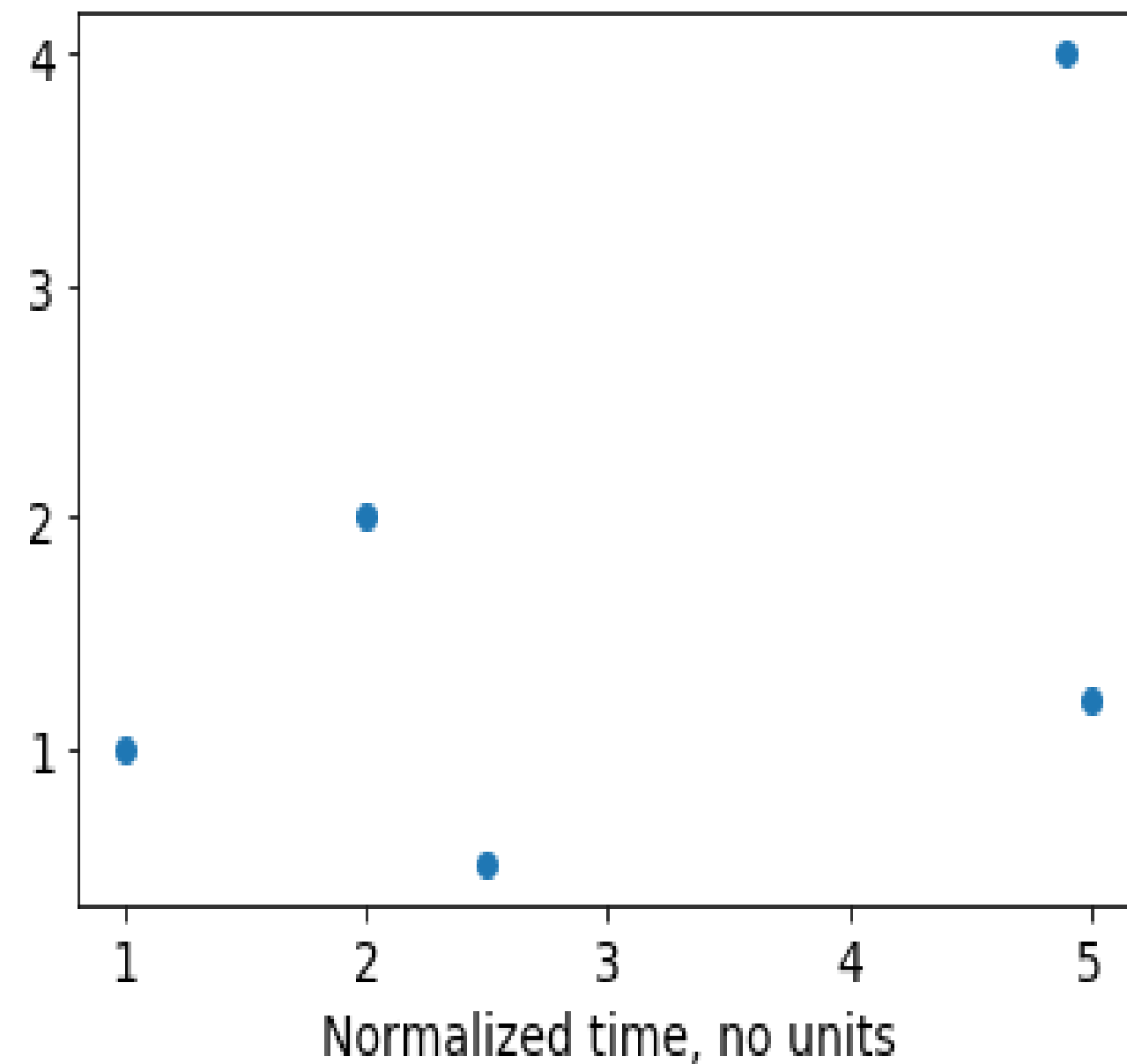
$$\mathbf{n}(t) = \frac{\mathbf{r} - \mathbf{r}_s(t)}{|\mathbf{r} - \mathbf{r}_s(t)|}$$



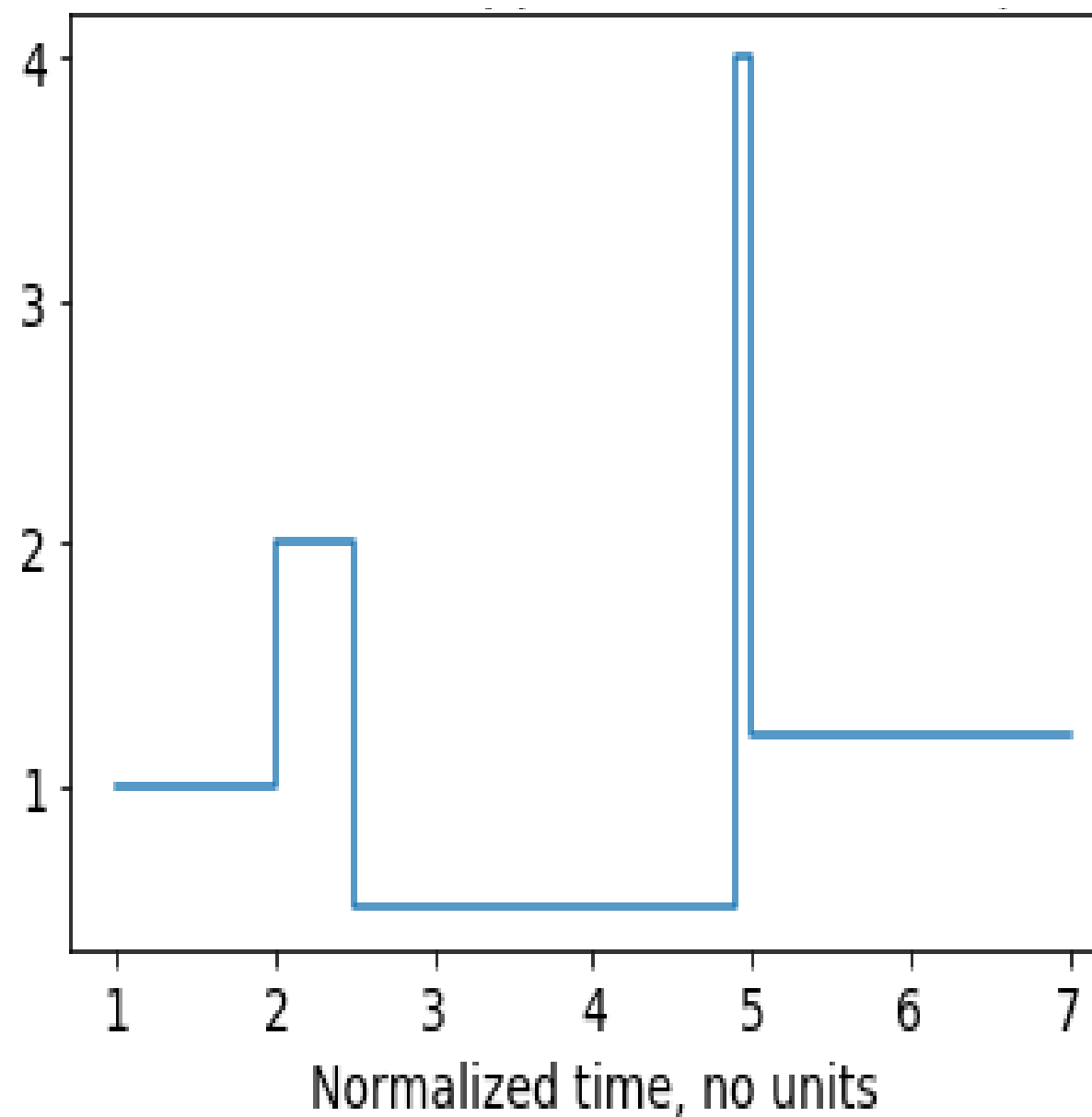
**ELECTRIC AND MAGNETIC FIELDS FOR EACH  
PARTICLE AT EACH SIMULATION STEP**

# SIMULATION STEP BY STEP

Track field after geant4



Approximated track field



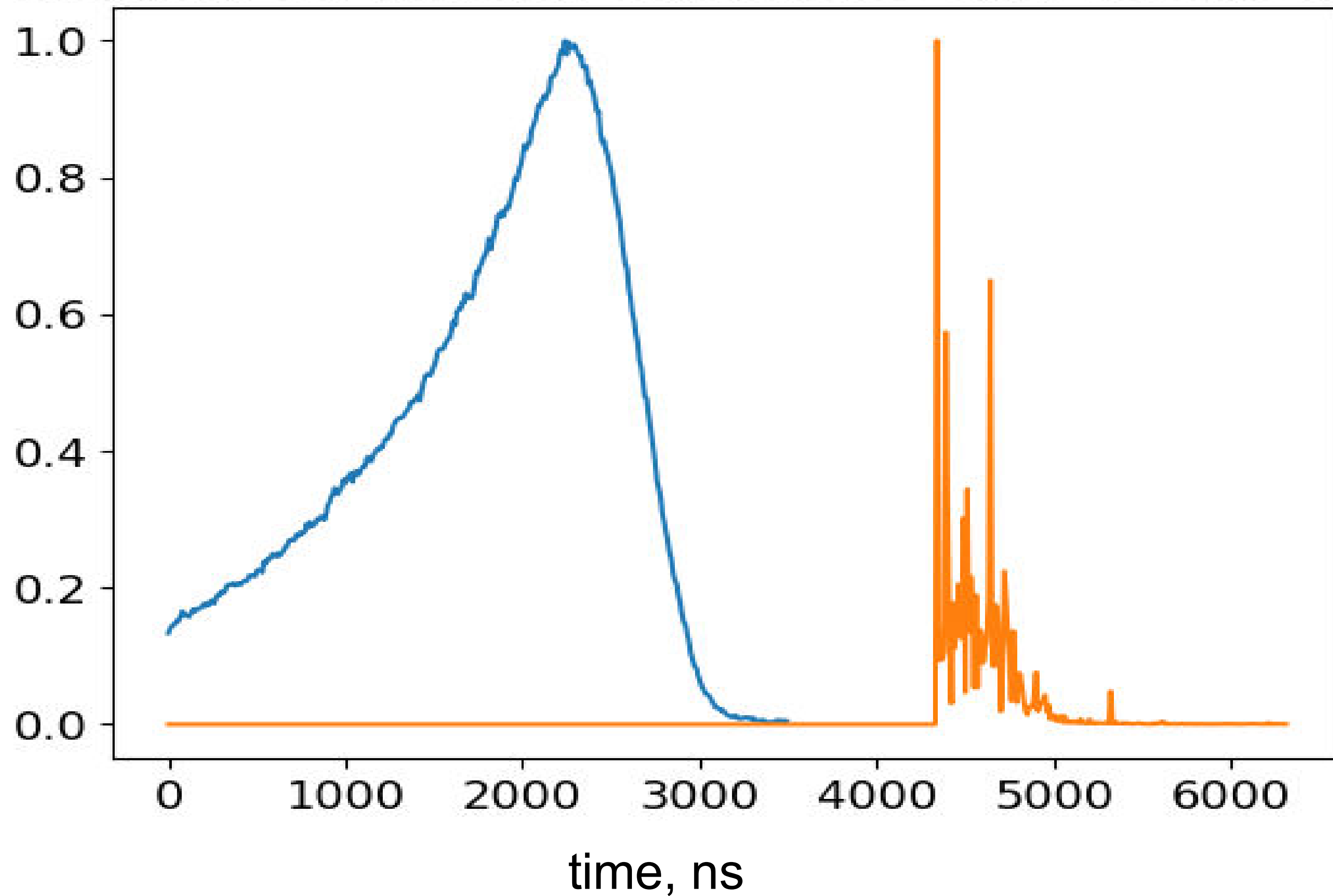
$$E_i = \sum_t^{M_i} E_t$$

$$E = \frac{\sum_i^N E_i}{N}$$

*i* - simulation number  
*E<sub>i</sub>* - field in *i*-simulation  
*N* - simulations amount  
*E<sub>t</sub>* - track field  
*t* - track number  
*M<sub>i</sub>* - simulation tracks amount

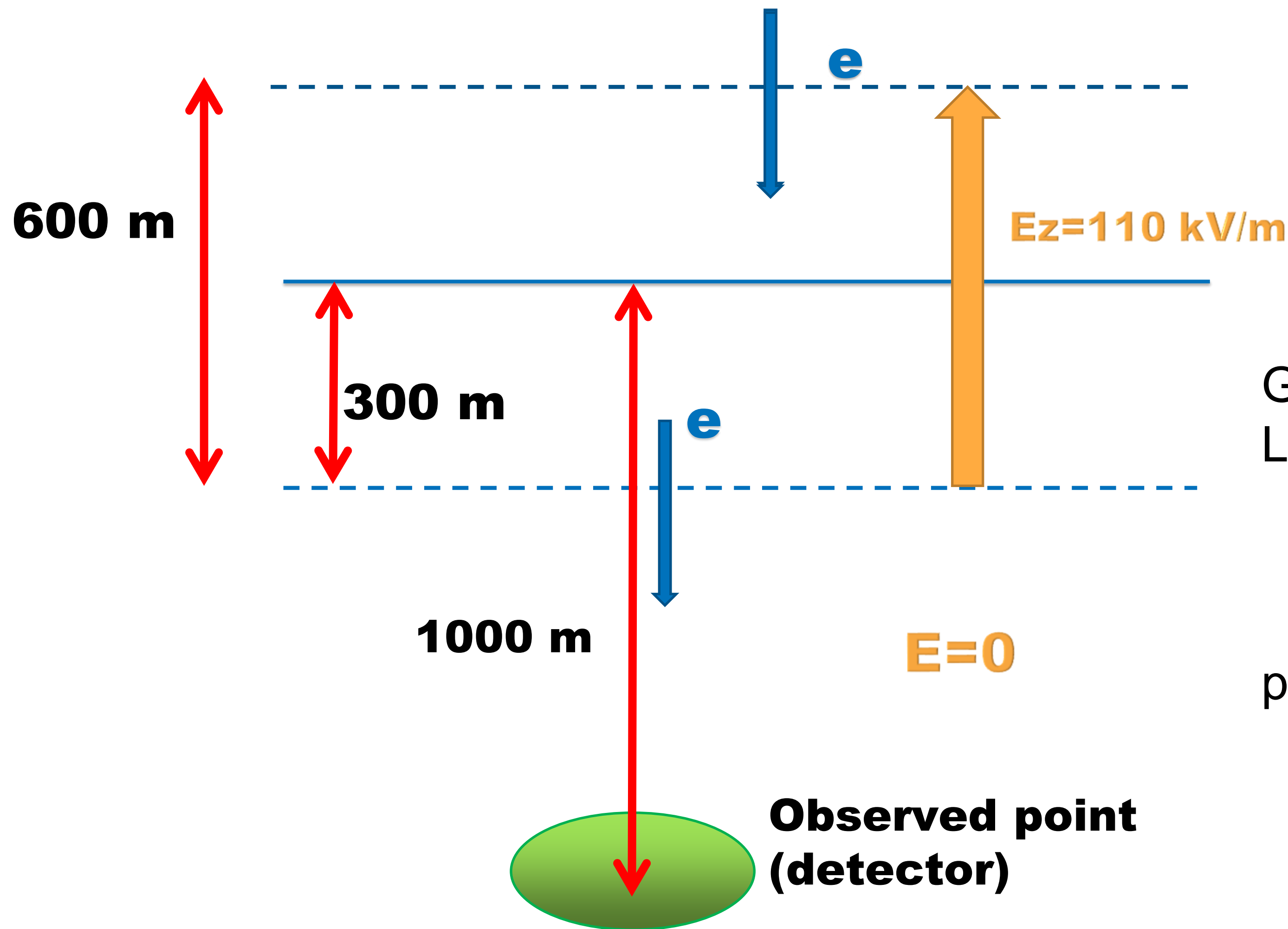
# DELAY AND COMPRESSION

normalized amount of particles and electric field



- **Amount of particles**
- **Electric field pulse**

# DELAY AND COMPRESSION



$H = 600\text{m}$  - cell size  
 $V = 0.8 \cdot C$  - electrons velocity for estimation  
 $h = 1000\text{m}$  - distance to observed point

Growth time =  $H/V = 2500 \text{ ns}$

Light arrival times:

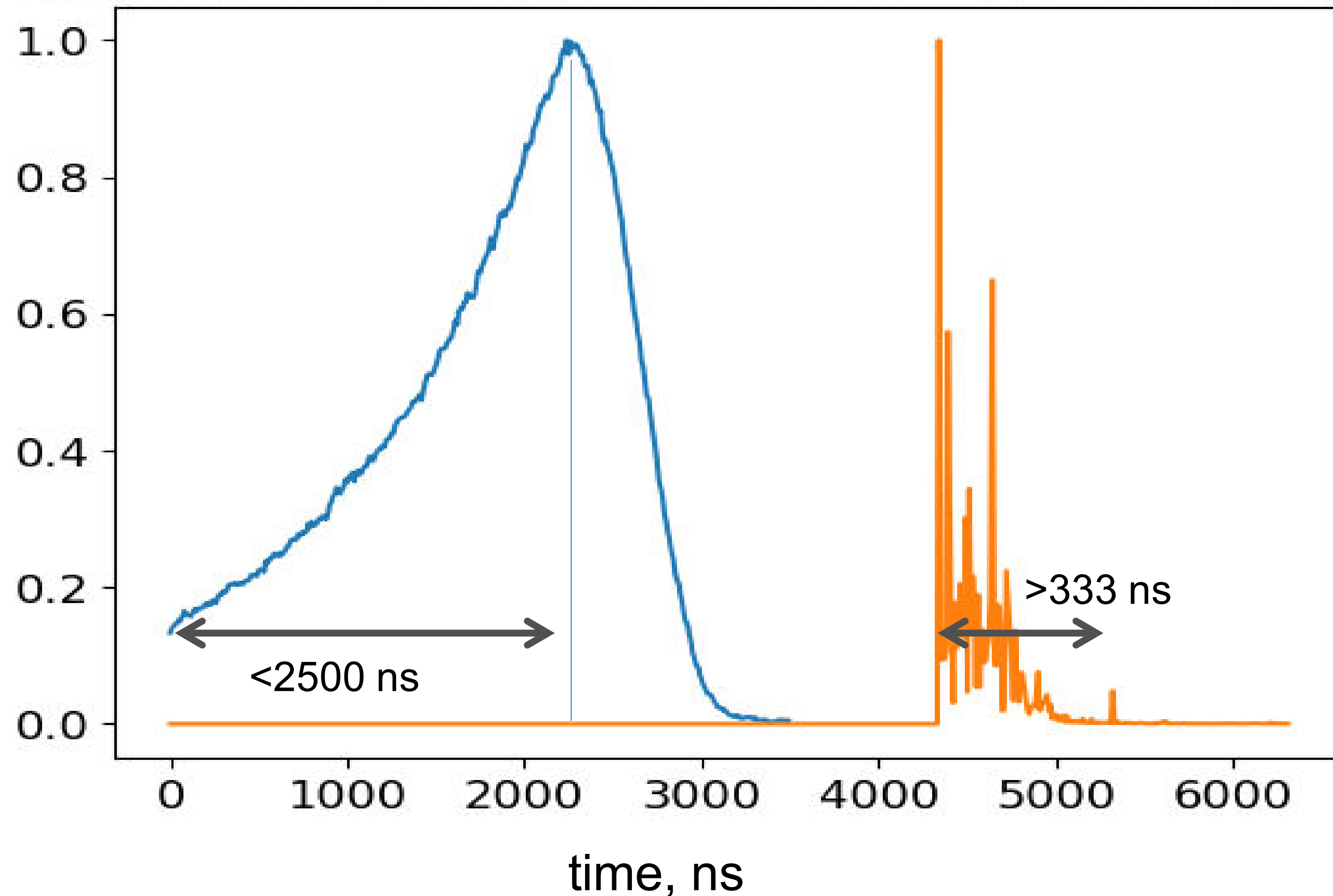
for seed electron =  $(H/2+h)/C \sim 4300 \text{ ns}$

for the last one =  $H/0.8C + (h-H/2)/C \sim 4633 \text{ ns}$

pulse duration  $> 4633 - 4300 = 333 \text{ ns}$

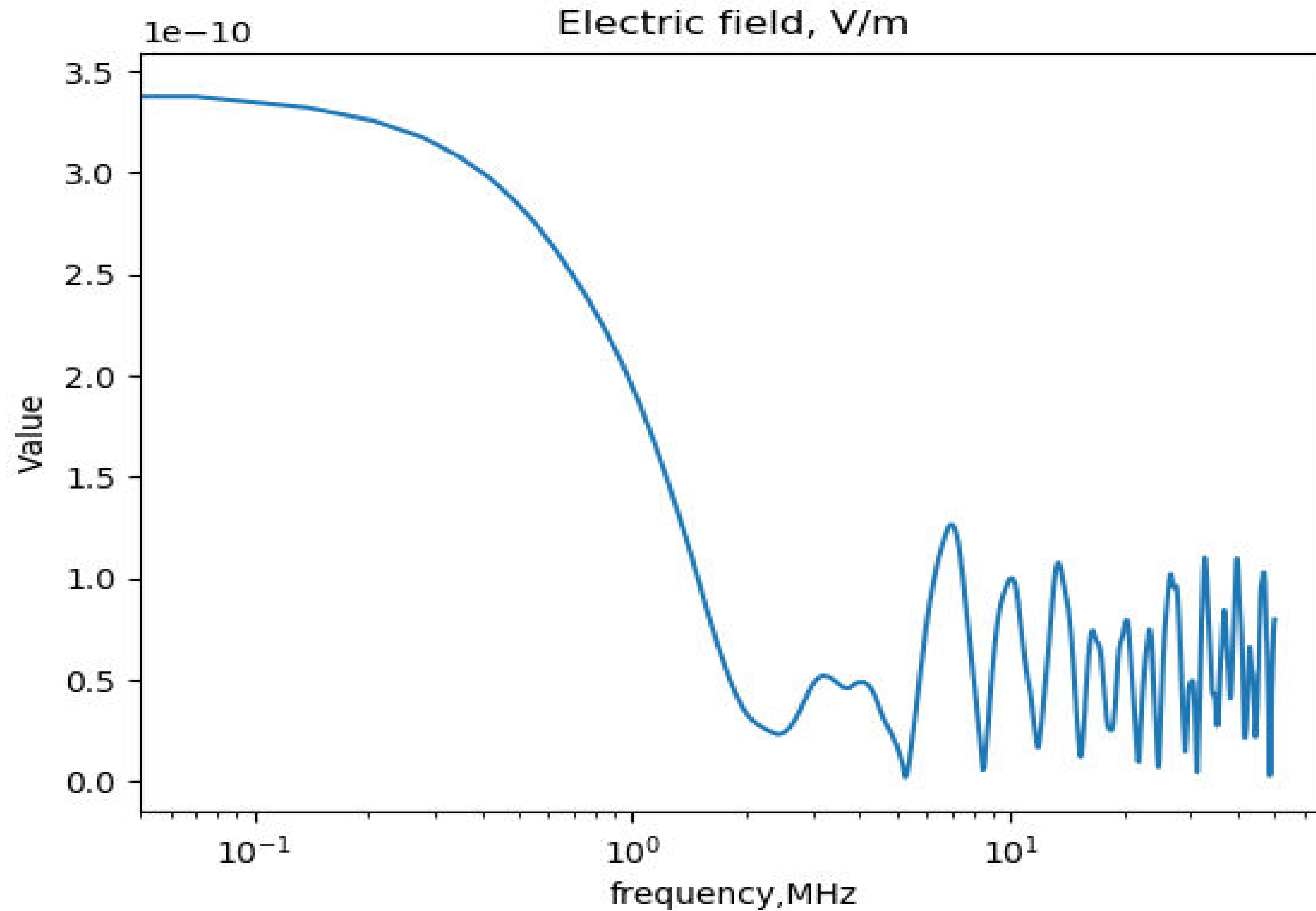
# DELAY AND COMPRESSION

normalized amount of particles and electric field



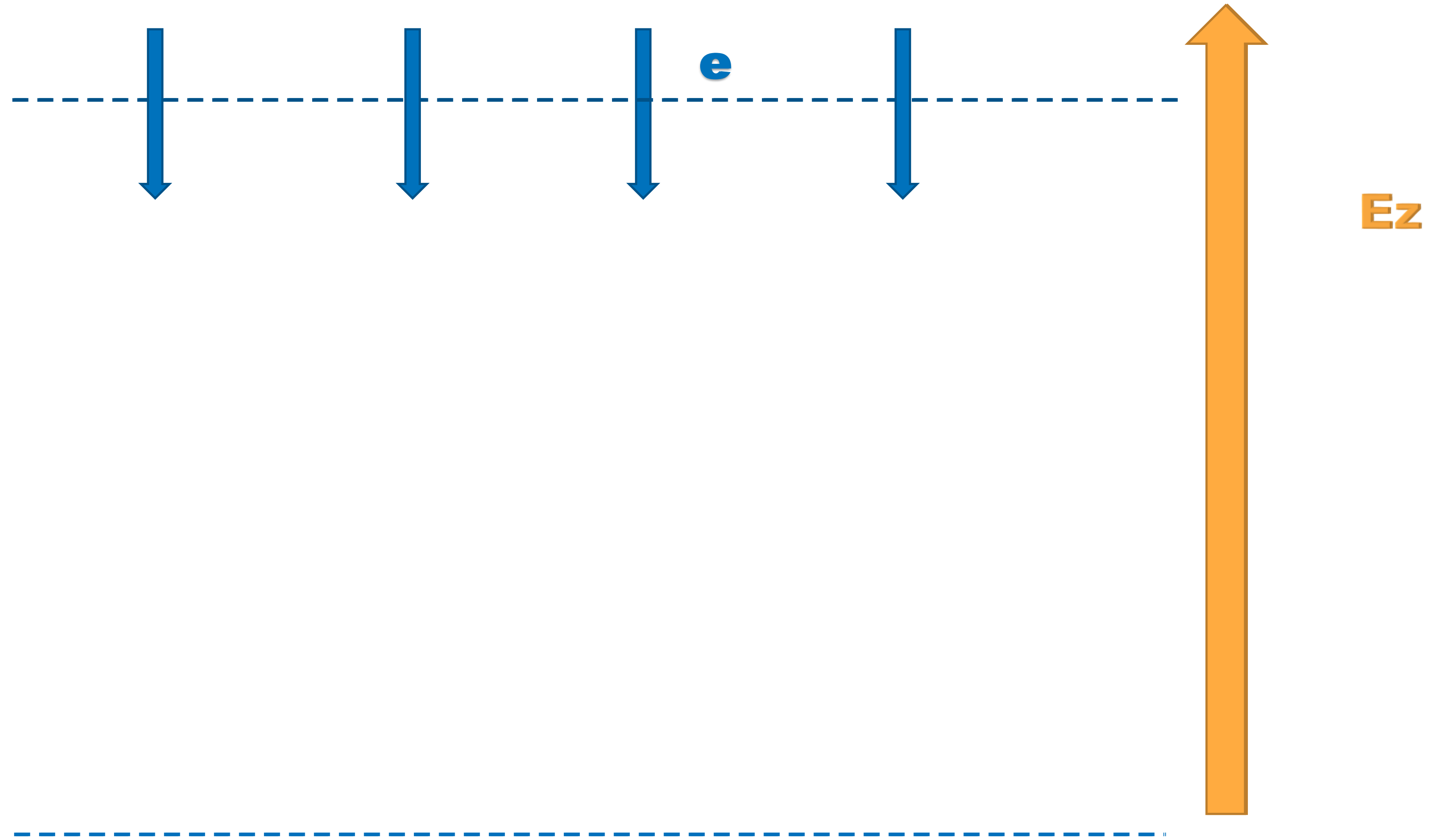
- Amount of particles
- Electric field pulse

# SPECTRUM

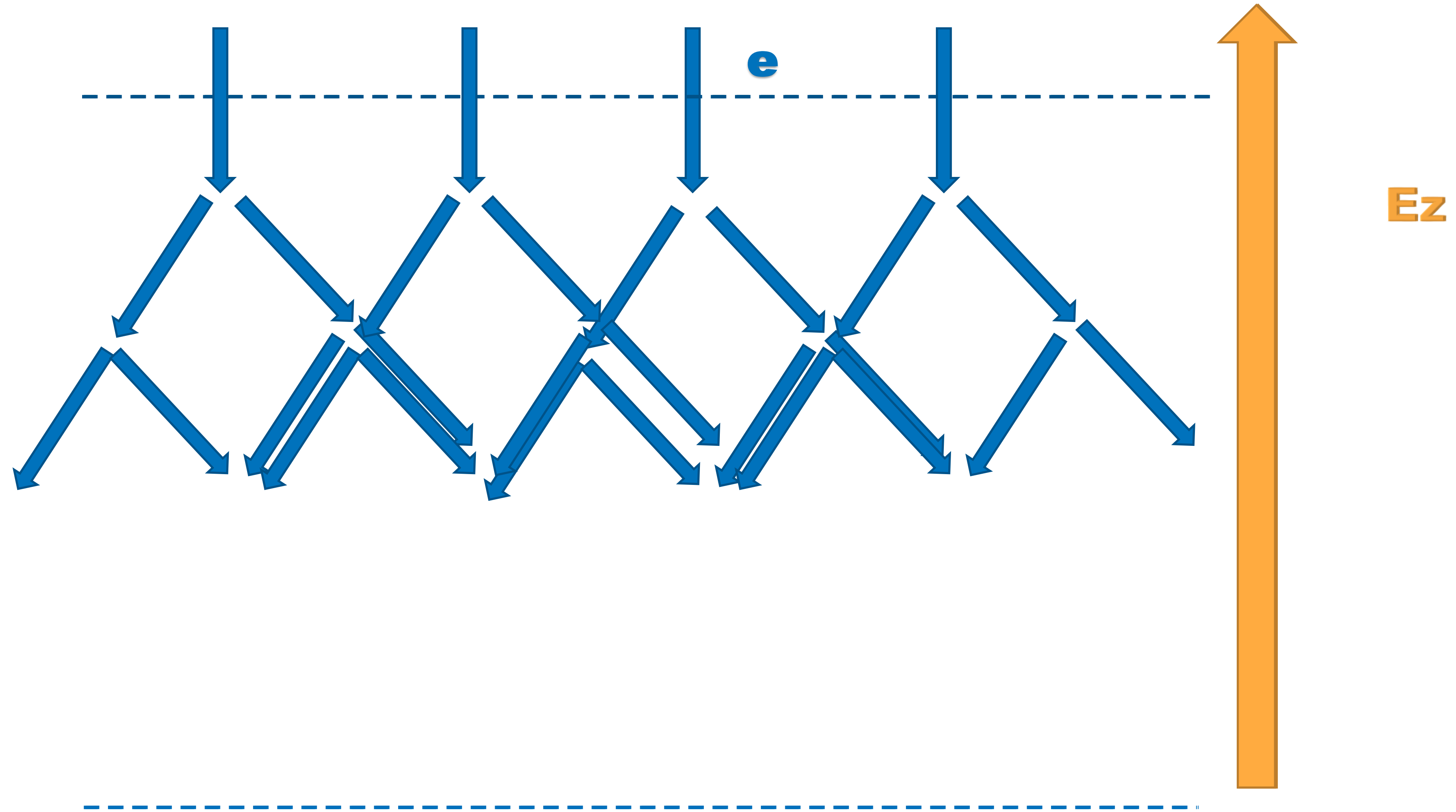




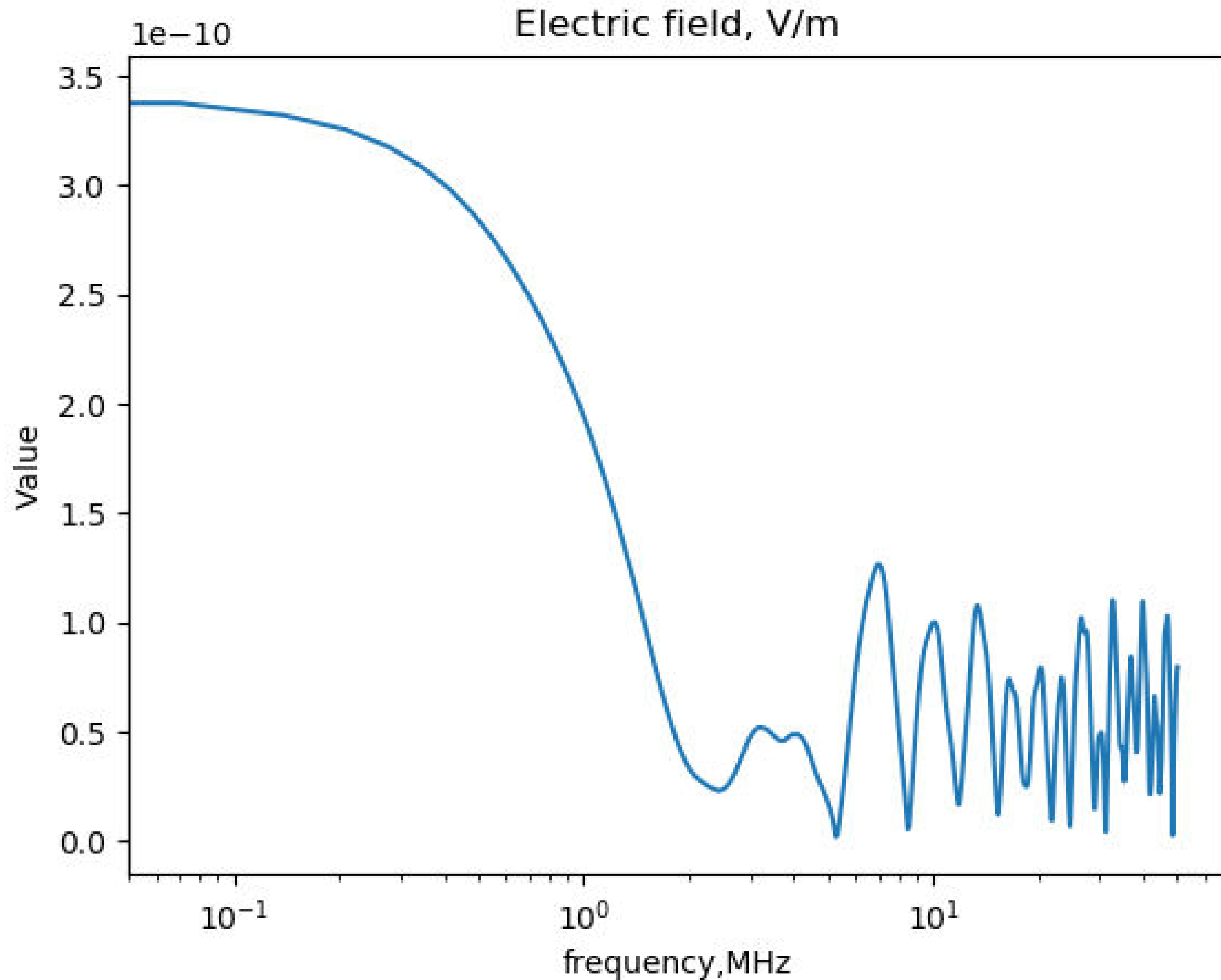
# RELATIVISTIC RUNAWAY ELECTRON AVALANCHE



# RELATIVISTIC RUNAWAY ELECTRON AVALANCHE



# SPECTRUM, MEASURABILITY



**Peak value  $3 \cdot 10^{-10}$  V/m is unmeasurable**

**Seed flux density is 1000 electrons per second per square meter \***

**Coherence time  $\sim 1000$  ns  $\rightarrow$**

**$\rightarrow$  seed flux 1000 electrons per square km per microsecond**

**Multiplied value  $\sim 3 \cdot 10^{-7}$  V/m**

\* Astrophysics and Space Science Library 303) Lev I. Dorman (auth.)-  
Cosmic Rays in the Earth's Atmosphere and Underground-Springer  
Netherlands (2004)

# MEASURABILITY: alternative estimation

$$E_z(r, t) = \frac{1}{2\pi\epsilon_0} \int_{h_1}^{h_2} \left[ dz \frac{(2z^2 - r^2)}{R^5(z)} \int_{t_b(z)}^t i\left(z, \tau - \frac{R(z)}{c}\right) d\tau \right. \\ \left. + \frac{(2z^2 - r^2)}{cR^4(z)} i\left(z, t - \frac{R(z)}{c}\right) dz \right. \\ \left. - \frac{r^2}{c^2 R^3(z)} \frac{di\left(z, t - \frac{R(z)}{c}\right)}{dt} dz \right],$$

R - distance to observed point

r - horizontal projection of R

h1, h2 - cell top and bottom heights

I - current , delta ~ 1 or 2 m

$I = e \cdot N \cdot V / (\text{delta})$

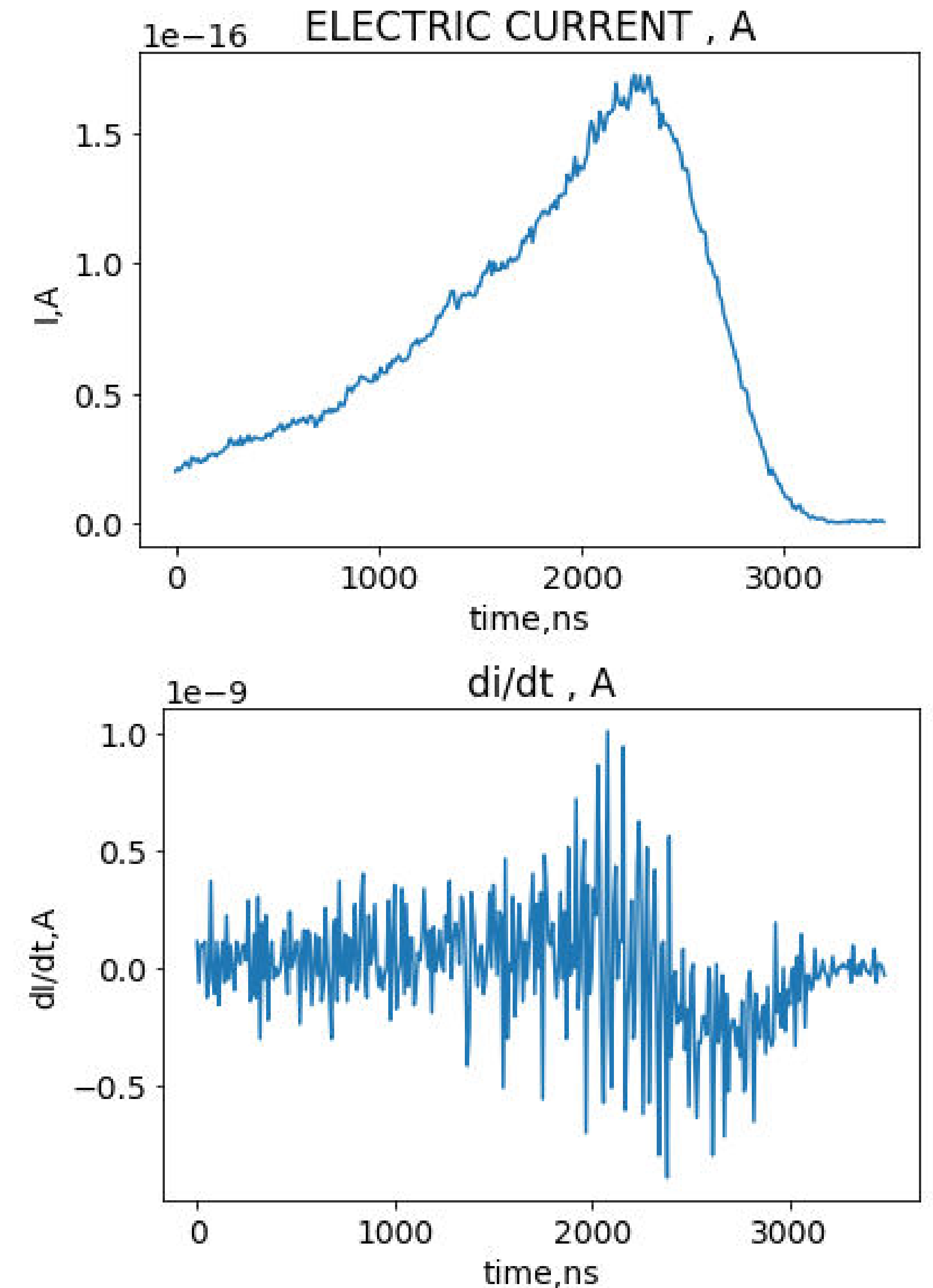
N - amount of particles in RREA

Amitabh Nag and Vladimir A. Rakov,  
JOURNAL OF GEOPHYSICAL  
RESEARCH, VOL. 115,  
D20102, doi:10.1029/2010JD014235, 2010

# MEASURABILITY: alternative estimation

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JOURNAL OF GEOPHYSICAL  
RESEARCH, VOL. 115,  
D20102, doi:10.1029/2010JD014235, 2010

R - distance to observed point

r - horizontal projection of R

h1, h2 - cell top and bottom heights

i - current

$di/dt = e \cdot dN/dt$ , N - amount of particles  
in RREA

r = 500m, R = 1000m,

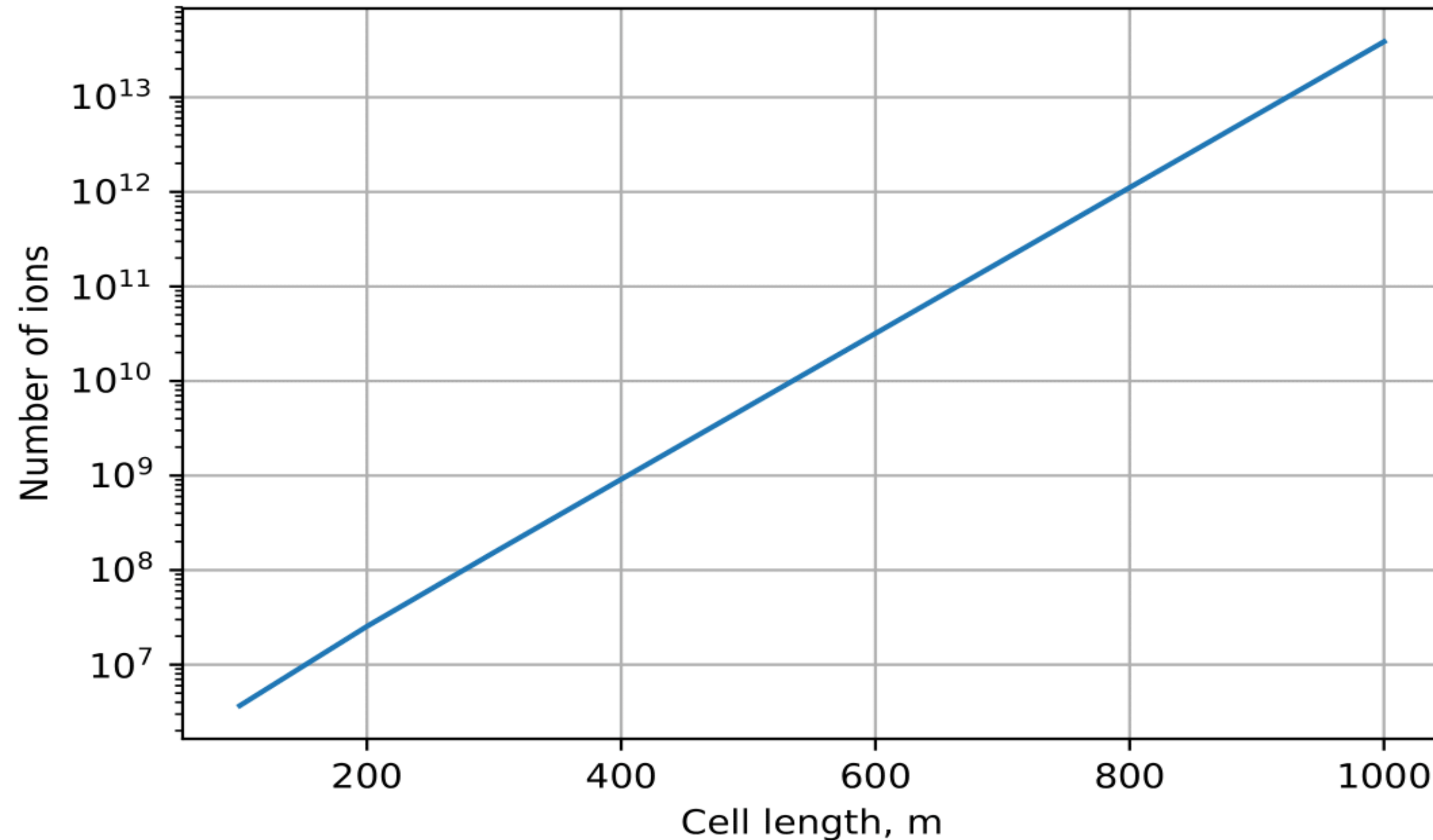
$di/dt = 10^{-9}$  A/s

h1 = 700m, h2 = 1300m

$\Rightarrow E \sim 10^{-10}$  V/m

# MEASURABILITY: low energy particles

Number of ions from RREA



$10^7 - 10^9$  times higher  
amount of particles

$10^6$  times lower velocity

# SUMMARY

High energy electrons can not produce measurable VHF signal

Low energy particles also unlikely to be the source of measurable radio waves

Observed pulses following RREA are something else



**THANKS FOR YOUR ATTENTION!**

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street

# MIPT at a glance



## Rankings

**#48** ★  
**THE**  
**Physics**

**#67** ★  
**THE Computer**  
**Science**

**#42** ★  
**QS Physics**  
**& Astronomy**

## Alumni

-  Yuriy Baturin  
Pilot astronaut, Hero of the Russian Federation
-  Alexander Kaleri  
Pilot astronaut, Hero of the Russian Federation
-  Konstantin Novoselov  
Nobel prizeman
-  Andrei Geim  
Nobel prizeman
-  David Yan  
Founder and Director of the board of ABBYY
-  Sergey Belousov  
Founder and CEO of Acronis

## Numbers

Founded in **1951**

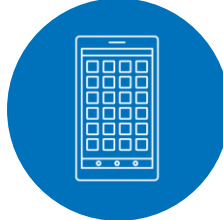

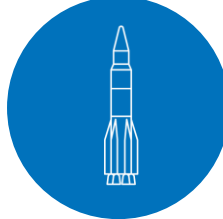





Nobel prizemen among professors and alumni

**80** Labs on campus

**7132** Students

## Phystech Schools

-  Radio Engineering and Computer Technology
-  Fundamental and Applied Physics
-  Aerospace Technology
-  Applied Mathematics and Informatics
-  Biological and Medical Physics
-  Electronics, Photonics and Molecular Physics